Applications of Metabolic Control Analysis

C1net Workshop 2; Day 3



dfell@brookes.ac.uk

http://mudshark.brookes.ac.uk



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- Understanding Feedback Inhibition
- Metabolism and Genetics
- Metabolism and Drug Action
- Enzyme overexpression
- Summary

- MCA continued:Feedback inhibition
- MCA and genetics
- MCA and drug action
- Enzyme over-expression



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- Feedback inhibition and control analysis
- Feedback inhibition and control analysis
- Properties of feedback inhibition
- Supply–Demand Analysis
- Flux control and metabolite homeostasis: the link
- Flux control and metabolite homeostasis: the link

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Classical biochemical theory proposed that feedback—inhibited enzymes at the start of a pathway were likely 'rate—limiting steps'.

Early opposition to Metabolic Control Analysis centered on the prediction by the latter that such enzymes would have low control coefficients.

One example of the experimental evidence follows; others will come later.

BROOKES Feedback-inhibited enzymes: ATCase

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Liu et al $(1993)^1$ showed that it took a 19–fold decrease in ATCase to produce a 1.8–fold decrease in growth rate attributable to pyrimidine biosynthesis. (= Approximate flux control coefficient of < 0.05.) Nevertheless, the authors state that:

Assuming that ATCase activity is the rate—limiting step in pyrimidine biosynthesis ... (a situation which is highly likely because of the enzyme's position in the pathway, its pattern of regulation and the toxicity of its product) ...

¹C. Liu et al, *J. Bacteriol.* 175, 2363–2369 (1993).

BROOKES UNIVERSITY Feedback inhibition and control analysis

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This is a generalized feedback inhibition loop, with the enzymes represented by numbered boxes. Metabolite S_3 inhibits enzyme 1.

BROOKES Feedback inhibition and control analysis



Feedback alters the control distribution. The flux control coefficients of enzymes 1 (curve a) and 4 (curve b) of the previous pathway are plotted against the inhibition constant for S_3 on enzyme 1 in this simulated example. The inhibition weakens from left to right.

BROOKES Properties of feedback inhibition

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- 1. Feedback inhibition is an antidote to the tendency of reactions at the start of a pathway to have the greater control of flux.
- 2. Feedback inhibition improves homoeostasis of the concentration of the feedback metabolite;increased cooperativity of the inhibition specifically enhances this effect.
- 3. Feedback inhibition improves the stability of pathways in that it speeds up the return to a steady state after random perturbation,

BROOKES Supply–Demand Analysis

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e.g. for a linear supply-demand pathway:

$$X_0$$
 — supply \rightarrow S — demand \rightarrow X_1

$$\frac{C_{supply}^S}{C_{supply}^J} = \frac{1}{\varepsilon_S^{demand}}$$

$$\frac{C_{demand}^S}{C_{demand}^J} = \frac{1}{\varepsilon_S^{supply}}$$

BROOKES Flux control and metabolite homeostasis: the



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Homeostasis of metabolite concentrations is not compatible with control located in the supply reactions. (Q = $-\varepsilon_S^{supply}/\varepsilon_S^{demand}$; 1: C_{supply}^J , 2 & 3: C_{supply}^S for two values of ε_S^{demand} .)

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Homeostasis of metabolite concentrations is compatible with control located in the demand reactions. (Q = $-\varepsilon_S^{supply}/\varepsilon_S^{demand}$; 1: C_{demand}^J , 2 & 3: C_{demand}^S for two values of ε_S^{supply} .)



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• MCA and genetics -2

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Typically 95% of loss—of—activity mutations are recessive in terms of functional phenotype, implying that the majority of enzymes have small flux control coefficients.

Conversely, rat liver hexokinase IV (glucokinase) has a flux control coefficient of ≈ 1 on liver glycogen synthesis. In humans, MODY–2 diabetes is linked to a mutation in this enzyme and shows co–dominance (i.e. heterozygotes show an intermediate phenotype).

BROCKES Hexokinase IV over-expression



Hexokinase IV was over-expressed in hepatocytes resulting in faster glycogen synthesis from glucose (Agius et al, J. Biol. Chem. 271, 30479–30486,



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BROOKES Example: Oxidative Phosphorylation

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From "Metabolic pathways of Biochemistry": http://www.gwu.edu/ mpb/index.html

BROOKES Inhibitor Titration

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From: Rossignol et al, (1999) J Biol Chem, 274, 33426-33432.

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BROOKES Flux v. Degree of Inhibition



BROOKES UNIVERSITY Inhibitor Titrations and Control Coefficients



From: Rossignol et al, (2000) Biochem J, 347, 45-53.

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(Results of Jean-Pierre Mazat's group, Bordeaux.)

BROOKES MCA and Drug Target Selection



 $C_{GART}^{J_{purine}} = 0.01$ (Results of Pogson's group, Wellcome.)

ROOKES Transketolase as a drug target

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Transketolase as a drug target

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Transketolase, in the pentose phosphate pathway has a requirement for thiamine as a cofactor. Cancer patients are often thiamine–deficient.

But transketolase has a control coefficient on growth of 0.9 in thiamine-depleted cells, so added thiamine drives nucleic acid synthesis and cancer growth.

Restoring normal thiamine levels increases cancer growth up to 164%. However, transketolase is therefore a potential target for cancer therapy .

Begona, C-A et al. Eur. J. Biochem 268 (2001) 4177-4182.



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(Rankin Small & Henrik Kacser, 1993)

The factor f by which the pathway flux will increase for an r fold increase in the amount of enzyme activity in a linear pathway is:

$$f = \frac{1}{1 - \frac{r-1}{r}C_E^J}$$

where C_E^J is the flux control coefficient of the enzyme E on the pathway flux, J.

OXFORD **BROOKES** Limitations on the flux response **UNIVERSITY**

Introduction										
Understanding Feedback Inhibition		-	¹⁰ [Т			1	I	
Metabolism and Genetics										
Metabolism and Drug Action			8	_					/	/ Η
Enzyme overexpression	4	_								/ /
Finite change theory		5								
 Limitations on the flux response 		5	6	_					50//	/ –
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Engineering yeast ethanol	.2	>							120/	
production	n	5	4						//29	
Control at Feedback–Inhibited		2	- T						// 10 /	
Enzymes	Ľ	-							// /	
Potato Tuber Glycolysis from Storeb									5	
• Over-expressing PFK in			2					///		_
potato tubers			~						2	
 Metabolite changes in 									Z	
transgenics										
 Flux control coefficients in 										
potatoes			0 -		• •	0 4		• •	• •	
Concentration control			0)	0.2	0.4		0.6	0.8	T
coefficients										
Summary					Flu	ux cont	rol c	oeffici	ent	

BROOKES Yeast Anaerobic Glycolysis

Introduction	glucose	
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Inhibition	G-6-P	
Metabolism and Genetics		pai
	F_6_P	1-3
Metabolism and Drug Action		off
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Enzyme overexpression	F–1,6–BP	
Finite change theory	\downarrow	ald
response	$DHAP \rightleftharpoons GAP$	tim
• Yeast Anaerobic Glycolysis		aandh
Engineering yeast ethanol	\checkmark	gapun
production	1,–BPG	
Control at Feedback–Inhibited	\downarrow	pgk
Enzymes Patata Tubar Glycolysis from	3_PG	10
Starch	514	
• Over-expressing PFK in	\downarrow	pgm
potato tubers	2–PG	
 Metabolite changes in 		eno
transgenics	\ ▶	CHO
Flux control coefficients in	PEP	
Polatoes	\downarrow	pk
coefficients	pyruvate	
	pyruvate	
Summary	\checkmark	PDH, ADH
	ethanol	

BROOKES Engineering yeast ethanol production

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Understanding Feedback	Over-production of glycolytic enzymes on multicopy plasmids						
Inhibition	Enzyme	(X WT)	EtOH flux				
Metabolism and Genetics			(XWT)				
Metabolism and Drug Action	HK	13.9	1.07				
Finite change theory Limitations on the flux	GPI	11.3	0.91				
response • Yeast Anaerobic Glycolysis	PFK	3.7	1.02				
 Engineering yeast ethanol production Control at Feedback–Inhibited 	PGK	7.5	0.97				
Enzymes	PGM	12.2	1.07				
Starch • Over-expressing PFK in potato tubers	PK	8.6	1.07				
 Metabolite changes in transgenics 	PD	3.7	0.85				
Flux control coefficients in potatoes	ADH	4.8	0.89				
 Concentration control coefficients 	PFK + PK	5.6+1.3	1.07				
Summary	PD + ADH	3.7 + 5.9	0.94				

Schaaff et al, Yeast 5, 285–290 (1989)

BROOKES Control at Feedback–Inhibited Enzymes

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The result for PFK suggests that its flux control coefficient is low. In addition, complementation of *pfk*- mutants with a non–allosteric enzyme from *D. discoideum* gave the same growth as wild–type.¹

No flux change was obtained with 30–fold amplification of the PEP–inhibited enzyme of potato tubers.²

This is consistent with predictions from control analysis. Kacser & Burns (1973) showed that feedback would transfer flux control downstream to steps utilising the feedback metabolite.

¹A. M. Estévez et al, FEBS Lett, 374, 100–104, (1995). ²M. Burrell et al, *Planta, 194*, 95–101 (1994); S. Thomas et al, *Biochem. J. 322*, 119–127 (1997).

BROOKES Potato Tuber Glycolysis from Starch

Introduction	glucose	
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Inhibition	G_1_P	
Metabolism and Genetics	\checkmark	pgm
	G–6–P	
Metabolism and Drug Action		nai
		P9'
Finite change theory	F-0-P	
Limitations on the flux	\downarrow	pfk
response	F-1.6-BP	
Yeast Anaerobic Glycolysis	,•	ماط
 Engineering yeast ethanol 	\checkmark	alu
production	$DHAP\rightleftharpoonsGAP$	tim
 Control at Feedback–Inhibited 		aapdh
Enzymes		3-1
Starch	I,-BFG	
• Over-expressing PFK in	\downarrow	pgk
potato tubers	3–PG	
 Metabolite changes in 		nam
transgenics	↓ - - - - - - - - - - -	pgm
Flux control coefficients in	2–PG	
potatoes	\downarrow	eno
coefficients	PEP	
coefficients		(1 1 - 1
Summary	\checkmark	'pk' etc
	pyruvate, TCA cycle etc	

BROOKES Over-expressing PFK in potato tubers

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Burrell et al (1994) Planta, 194, 95-101.

BROOKES Metabolite changes in transgenics

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• Read all about it!



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- Enzymes experiencing feedback inhibition have low flux control coefficients.
- Metabolite homeostasis is the dominant function of many control mechanisms, including feedback inhibition.
- It's hard to increase metabolic flux by activating/overexpressing a single enzyme.



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